

# A New General Model for Predicting Melting Thermodynamics of Complementary and Mismatched B-Form Duplexes Containing Locked Nucleic Acids: Application to Probe Design for Digital PCR Detection of Somatic Mutations

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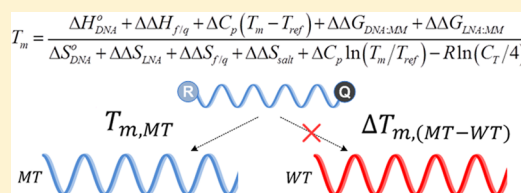
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## S Supporting Information

**ABSTRACT:** Advances in real-time polymerase chain reaction (PCR), as well as the emergence of digital PCR (dPCR) and useful modified nucleotide chemistries, including locked nucleic acids (LNAs), have created the potential to improve and expand clinical applications of PCR through their ability to better quantify and differentiate amplification products, but fully realizing this potential will require robust methods for designing dual-labeled hydrolysis probes and predicting their hybridization thermodynamics as a function of their sequence, chemistry, and template complementarity. We present here a nearest-neighbor thermodynamic model that accurately predicts the melting thermodynamics of a short oligonucleotide duplexed either to its perfect complement or to a template containing mismatched base pairs. The model may be applied to pure-DNA duplexes or to duplexes for which one strand contains any number and pattern of LNA substitutions. Perturbations to duplex stability arising from mismatched DNA:DNA or LNA:DNA base pairs are treated at the Gibbs energy level to maintain statistical significance in the regressed model parameters. This approach, when combined with the model's accounting of the temperature dependencies of the melting enthalpy and entropy, permits accurate prediction of  $T_m$  values for pure-DNA homoduplexes or LNA-substituted heteroduplexes containing one or two independent mismatched base pairs. Terms accounting for changes in solution conditions and terminal addition of fluorescent dyes and quenchers are then introduced so that the model may be used to accurately predict and thereby tailor the  $T_m$  of a pure-DNA or LNA-substituted hydrolysis probe when duplexed either to its perfect-match template or to a template harboring a noncomplementary base. The model, which builds on classic nearest-neighbor thermodynamics, should therefore be of use to clinicians and biologists who require probes that distinguish and quantify two closely related alleles in either a quantitative PCR or dPCR assay. This potential is demonstrated by using the model to design allele-specific probes that completely discriminate and quantify clinically relevant mutant alleles (*BRAF* V600E and *KIT* D816V) in a dPCR assay.



Dual-labeled hydrolysis probes are widely used by clinics in real-time quantitative PCR (qPCR) assays, and more recently in digital PCR (dPCR) assays, to detect germline variations or somatic mutations associated with diseases, including various types of cancer, and thereby facilitate diagnosis and subtyping of disease, setting of treatment regimens, and monitoring of minimal residual disease levels following treatment.<sup>1</sup> These assays are often designed to detect a specific somatic mutation present in a rare population of abnormal or tumor cells dispersed within a tissue matrix abundant in normal cells carrying the homologous wild type (germline) allele.

The use of qPCR to distinguish between two alleles that differ greatly in abundance while differing in sequence by as

little as a single base pair often requires the engineering of a probe that displays high affinity and specificity for the low-abundance mutant (MT) allele and little to no affinity for the closely related wild type (WT) gene at the qPCR annealing temperature ( $T_a$ ). This in turn requires a sufficiently large difference ( $\Delta$ ) between  $T_{m,MT}$ , the melting temperature ( $T_m$ ) of the perfectly matched duplex formed by the probe and its MT target, and  $T_{m,WT}$ , the  $T_m$  for the mismatched duplex formed by the probe and the more abundant WT gene. The

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thermodynamics of bimolecular complexation equilibria provide the necessary conditions for achieving this goal:

$$\begin{aligned}\Delta T_{m,(MT-WT)} &= T_{m,MT} - T_{m,WT} \\ &= \frac{\Delta H_{MT}}{\Delta S_{MT} - R \ln(C_{T,MT}/2)} \\ &\quad - \frac{\Delta H_{WT}}{\Delta S_{WT} - R \ln(C_{T,WT}/2)}\end{aligned}\quad (1)$$

where  $\Delta H$  and  $\Delta S$  are the enthalpy change and entropy change, respectively, for the helix-to-coil transition of a duplex formed from two single strands, each of which is non-self-complementary.  $\Delta H$  and  $\Delta S$  are both positive in value for the probe:MT or probe:WT duplex denaturation reaction; if the heat capacity change ( $\Delta C_p$ ) for the denaturation reaction is ignored,  $\Delta H$  and  $\Delta S$  may also be taken to be independent of temperature.  $C_T$  is the total strand concentration, probe plus template, and both  $C_{T,MT}$  and  $C_{T,WT}$  in eq 1 are equal to  $C_{probe}$  in assays of this type because the probe is present in great excess relative to either template at the start of the reaction. The concentration ( $C_T$ ) is divided by 2 in eq 1 because the large excess of probe renders the hybridization reaction pseudo-first-order. As a result,  $R \ln(C_{T,MT}/2)$  and  $R \ln(C_{T,WT}/2)$  can, for the sake of simplicity, be denoted by a constant  $C$  that is set by  $C_{probe}$ . Achieving an acceptable  $\Delta T_{m,(MT-WT)}$  therefore requires a probe for which  $\Delta H_{MT}/(\Delta S_{MT} + C) > T_a > \Delta H_{WT}/(\Delta S_{WT} + C)$ . This thermodynamic criterion is difficult to realize, as melting transitions occur across a range of temperatures and  $\Delta T_{m,(MT-WT)}$  is often less than 6 °C, in part because of the relatively small proportional contribution of a single base pair to the overall thermodynamic stability of a duplex formed with a standard 20–25 bp pure-DNA probe. Current strategies for realizing a suitable  $\Delta T_{m,(MT-WT)}$  therefore involve modifying oligonucleotides used as hydrolysis probes either by adding a 3'-terminal minor groove binder (MGB) ligand<sup>2</sup> or by replacing nucleotides within the probe with their corresponding locked nucleic acid (LNA) analogue.<sup>3,4</sup> The latter approach can increase the difference in MT and WT duplex stabilities through the ability of LNA substitutions to decrease probe length while maintaining  $T_{m,MT}$ ,<sup>4,5</sup> and the generally greater energetic intolerance of LNAs to participate favorably in mismatched base pairs.<sup>6</sup> LNA-bearing probes have therefore been shown to offer specific advantages when applied to the detection of either germline variants, including single-nucleotide polymorphisms (SNPs),<sup>4,7,8</sup> or acquired variants, including somatic point mutations (SPMs).<sup>9–11</sup>

MGB- and LNA-modified probes can demonstrate comparable performance in qPCR genotyping assays.<sup>3</sup> For example, a 15-mer probe coupled to an MGB linker<sup>12,13</sup> and a 16-mer LNA-bearing<sup>9</sup> probe provide an equivalent limit of detection (LOD) of 1–2% (relative to the abundance of the WT allele in the specimen) when applied to the detection of the V617F somatic mutation within the human *JAK2* gene. The *JAK2* V617F mutation is often found in Philadelphia chromosome negative myeloproliferative neoplasm (MPN) patients,<sup>14</sup> including at high incidence in patients with polycythemia vera (PV), essential thrombocythemia (ET), or idiopathic myelofibrosis (IMF). Most cancer clinics therefore test for *JAK2* V617F on human chromosome 9 to identify MPN and leukemia patients and define appropriate treatment regimens.<sup>15</sup> Improving V617F mutational analysis could therefore provide for early

or more sensitive diagnoses of PV, as well as related MPDs and leukemias.

Guidelines for designing probes bearing one or more LNA substitutions have been proposed.<sup>6</sup> Recently, we reported a molecular thermodynamic model that accurately predicts melting temperatures and thermodynamic changes under standard thermodynamic conditions (pH 7, 1 M NaCl) for short perfectly complementary duplexes containing any combination of LNA substitutions in one strand.<sup>16</sup> Other models have recently been proposed for this purpose, as well.<sup>17–19</sup> Here, we define differences between these models and when they become important and then show how our model may be extended to introduce two additional capabilities useful for designing probes bearing one or more LNA substitutions: namely, the ability to accurately predict under PCR solution conditions (1) the  $T_m$  value for any complementary duplex formed between a dual-labeled LNA-substituted probe and its target allele and (2) the value of  $\Delta T_{m,(MT-WT)}$ , which is needed to ensure that the probe hybridizes only to its target allele during qPCR amplification. The intent is to establish a simple, reliable method for accurately predicting  $T_m$  and  $\Delta T_{m,(MT-WT)}$  for pure-DNA and LNA-substituted hydrolysis probes operating under standard and PCR-relevant conditions.

Melting thermodynamics data collected by thermal-ramp ultraviolet “melt” spectroscopy (UVM) are reported for a large set of pure-DNA and LNA-containing oligonucleotides that are either perfectly complementary to their duplexed template or form a mismatched DNA:DNA or LNA:DNA base pair with the template. The data are used to regress the model parameters needed to accurately predict from sequence information the melting thermodynamics of complementary or mismatched pure-DNA or LNA-substituted duplexes under standard thermodynamic conditions. In addition, we report UVM data for a large set of LNA-substituted oligonucleotides bearing a 5'-fluorescence reporter dye (e.g., FAM or HEX) and a 3'-fluorescence quencher [e.g., Black-Hole Quencher 1 (BHQ1)] duplexed either to their perfect complement or to a template containing a single mismatch. Those data are used to extend the model to allow accurate prediction of  $\Delta T_{m,(MT-WT)}$  under PCR-relevant conditions.

We show the resulting model can be used to define LNA substitution patterns on a probe, as well as probe positions on a template, that create a  $T_{m,MT}$  and  $\Delta T_{m,(MT-WT)}$  that permit efficient hybridization to a target MT allele while limiting probe duplexation with a nontarget WT allele under PCR conditions. This novel model-driven design strategy demands accurate prediction of hybridization thermodynamics, and we therefore validate results from our model against experiment for a large set of model-designed probes. Model-designed unlabeled and dual-labeled hydrolysis probes offering large  $\Delta T_{m,(MT-WT)}$  values are created against a number of somatic point mutation “hot spots” for various genes (*BRAF*, *EGFR*, *JAK2*, *KIT*, *PIK3CA*, *PTEN*, and *TP53*) that are clinically relevant in cancer monitoring and treatment. Finally, application of model-refined probes against *BRAF* V600E and *KIT* D816V in a droplet digital PCR (ddPCR) format is shown to result in complete segregation of data fields to permit quantitative detection of the mutant allele.

## MATERIALS AND METHODS

**Oligonucleotides.** All DNA and LNA oligonucleotides used as templates or primers in UV melting (UVM)

experiments or in droplet digital PCR (ddPCR) assays were synthesized and purified through standard desalting by either Prologo/Sigma-Aldrich (St. Louis, MO) or Integrated DNA Technologies (IDT, Coralville, IA). All unlabeled and dual-labeled hydrolysis probes were purchased from either Exiqon Inc. (Vedbæk, Denmark) or IDT and purified by high-performance liquid chromatography (HPLC). Mini-gene plasmids were synthesized by IDT and used to represent the *BRAF* WT or V600E and *KIT* WT or D816V alleles. *BRAF* plasmids were ampicillin resistant and also of pUC origin and included a 280 bp fragment of *BRAF* spanning from intron 14 to 15, thru exon 15, and into introns 15 and 16. The *KIT* plasmids were kanamycin resistant and of pUC origin and contained a 335 bp segment of *KIT* spanning portions of introns 16 to 17 and 17 to 18, and all of exon 17.

Primer sets used for amplification of the *BRAF* WT and V600E plasmids included the forward primer (FP) 5'-ctactgtttcttcttacttactacacctcaga-3' and reverse primer (RP) 5'-agctcaattcttaccatcca-3', while those used for *KIT* WT and D816V plasmids included FP 5'-ctcctccaacctaagtgtattcacag-3' and (RP) 5'-gcagagaatgggtactcacg-3'. Both forward and reverse primer sets were designed to hybridize to appropriate intron/exon boundary regions within a mini-gene template sequence of the target gene displayed on a plasmid. Amplicon lengths for *BRAF* and *KIT* were 164 and 158 bp, respectively.

**Monitoring Helix-to-Coil Transitions via UVM Spectroscopy.** UVM profiles for the thermally induced melting of complementary or mismatched duplexes composed of either pure DNA or DNA containing LNA substitutions in one strand were collected at an absorbance wavelength of 260 nm using a Varian Inc. (Santa Clara, CA) Cary 1E spectrophotometer equipped with a 12-cell Peltier temperature controller. The two strands were combined at an equimolar concentration to reach a total strand concentration ( $C_T$ ) sufficient for UVM-based melt analysis. For melting experiments conducted under standard thermodynamic solution conditions, perfect match or mismatched duplexes were resuspended to a  $C_T$  of 2, 50, or 100  $\mu$ M in 10 mM  $\text{Na}_2\text{HPO}_4$  (pH 7.0) buffer containing 1 M NaCl and 1 mM  $\text{Na}_2\text{EDTA}$ . UVM data were also collected under PCR conditions in a buffer containing New England Biolabs (Ipswich, MA) 1 $\times$  Taq standard reaction buffer and  $\text{MgCl}_2$  to form a solution with final  $\text{MgCl}_2$  and KCl concentrations of 3 and 50 mM, respectively. UVM experiments involving dual-labeled hydrolysis probes and their corresponding template were performed at a  $C_T$  of 2, 5, or 10  $\mu$ M in this buffer.

Duplex samples were annealed prior to UVM data collection by preheating the sample to a temperature between 75 and 95  $^\circ\text{C}$ , holding it for 3 min, and slowly cooling it to a temperature between 15 and 25  $^\circ\text{C}$ . The equilibrated samples were then loaded into quartz cuvettes with path lengths of 10 or 1 mm and sealed with fitted caps to prevent evaporation during heating. UVM experiments were conducted by collecting absorbance readings at 260 nm ( $A_{260}$ ) every 0.5  $^\circ\text{C}$  as the temperature was increased from 5 to 95  $^\circ\text{C}$  at a rate of 0.5  $^\circ\text{C}/\text{min}$  to create a raw absorbance ( $A_{260}$ ) versus temperature ( $T$ ) profile, also known as a melt profile.

Raw UVM data were exported into Microsoft Excel and, in cases where a complete melting transition was recorded, used to compute the melting temperature and duplex-to-random coil state transition thermodynamics according to the procedures described by Hughesman et al.<sup>16</sup>

$T_m$  values for the mismatched duplexes were often too low ( $<30$   $^\circ\text{C}$ ) to permit collection of a complete melting transition by the UVM method. In these cases, the  $T_{\text{max}}$  value, which could be determined accurately from the maximum of the  $dA_{260}/dT$  data obtained, was instead recorded.

**Regression of  $\Delta\Delta G_{\text{LNA:MM}}$  Parameters.** Incremental  $\Delta\Delta G_{\text{LNA:MM}_i}$  model parameters, which define the change in Gibbs energy of a duplex resulting from the introduction of mismatched LNA:DNA base pairs, were determined through model regression to UVM-derived  $T_{\text{max}}$  and  $\Delta T_{\text{max}}$  data for those members among a set of 192 9-mer duplexes for which both values could be measured accurately (Table S1 of the Supporting Information). Although  $T_{\text{max}} \neq T_m$ ,  $\Delta T_{\text{max}}$  and  $\Delta\Delta T_{\text{max}}$  values provide very good estimates of  $\Delta T_m$  and  $\Delta\Delta T_m$ , respectively, and were applied in that manner.<sup>20,21</sup>  $\Delta\Delta G_{\text{LNA:MM}_i}$  parameters could then be determined through standard  $\chi^2$  minimization based on model regression to the complete set of  $\Delta\Delta T_m$  data

$$\chi^2 = \sum_i [\Delta\Delta T_{m(\text{Pred})_i} - \Delta\Delta T_{m(\text{Expt})_i}]^2 \quad (2)$$

where

$$\begin{aligned} \Delta\Delta T_{m_i} &= \Delta T_{m(\text{LNA-LNA:MM})_i} - \Delta T_{m(\text{DNA-DNA:MM})_i} \\ &= [T_{m(\text{LNA})} - T_{m(\text{LNA:MM})}]_i - [T_{m(\text{DNA})} - T_{m(\text{DNA:MM})}]_i \end{aligned} \quad (3)$$

$\Delta\Delta T_{m(\text{Expt})_i}$  was determined by collecting  $\Delta\Delta T_{m(\text{LNA-LNA:MM})_i}$  and  $\Delta T_{m(\text{DNA-DNA:MM})_i}$  data for each duplex sequence set  $i$ . The mean experimental errors for each  $\Delta T_m$  value were determined from two upscans and two downscans and are reported in Table S1 of the Supporting Information.  $\Delta\Delta T_{m(\text{Pred})}$  was determined by using the specified model to calculate values for  $T_{m(\text{LNA})}$ ,  $T_{m(\text{LNA:MM})}$ ,  $T_{m(\text{DNA})}$ , and  $T_{m(\text{DNA:MM})}$ . The model developed in this work cannot solve for  $T_m$  explicitly (see below). A Newton–Raphson type iteration implemented in Excel was therefore applied. Convergence of the model-predicted  $T_m$  value (generally within 0.1  $^\circ\text{C}$ ) was typically reached in two iterations, permitting straightforward determination of  $\Delta\Delta G_{\text{LNA:MM}_i}$  parameters using the method described above.

**Droplet Digital PCR Detection of *BRAF* V600E or *KIT* D816V.** Standard qPCR assays directed against an SPM-bearing MT allele typically require two competing dual-labeled hydrolysis probes, with each targeting either the WT or MT allele, to both reduce cross hybridization effects and permit quantification of relative abundances.<sup>22</sup> In principle, however, the need for competing probes to detect rare MT alleles may be relaxed in dPCR because of the ability to partition WT and MT alleles into separate droplets.<sup>23</sup> Quantification of mutation frequencies may then be achieved using a FAM-labeled probe against the mutant allele that spans the site of variance. Within the same reaction, total copies of all forms of the target gene, MT + WT, may be quantified using a HEX-labeled consensus probe designed to hybridize to a highly conserved region within an exon of the gene. One then counts those droplets containing an end-point HEX amplification signal to compute the total number of copies of the target gene in the sample and then counts the segregated cluster of droplets containing both an end-point HEX and FAM signal to compute the mutation frequency.



To test this concept, plasmids harboring the *BRAF* or *KIT* template were linearized using restriction enzyme *Cla*I or *Sph*I, respectively, at a single junction outside the amplicon region prior to ddPCR amplification. The assay workflow followed methods described previously.<sup>24</sup> A 20  $\mu$ L PCR mixture consisting of 10  $\mu$ L of 2 $\times$  dPCR Supermix for Probes (no dUTP) (Bio-Rad Inc., Hercules, CA), 2  $\mu$ L of 10 $\times$  primer and probe mix (to yield final concentrations of 900 nM primer and 200–250 nM probe), and 8  $\mu$ L of template (to yield on average 300 *BRAF* copies or 100 *KIT* copies per microliter) was loaded into each sample well of an eight-channel disposable droplet generation cartridge (Bio-Rad); 60  $\mu$ L of QX100 Droplet Generation Oil (Bio-Rad) was then loaded into the corresponding oil well. A droplet-containing emulsion was generated according to the manufacturer's instructions (Bio-Rad), and 40  $\mu$ L droplets in excess oil were transferred manually into a 96-well PCR plate (Eppendorf, Hamburg, Germany). The plate was heat sealed (Eppendorf) with foil and amplified to end point in a CFX96 thermocycler (Bio-Rad). Thermocycling conditions included activation at 95  $^{\circ}$ C for 10 min (one cycle), denaturation at 94  $^{\circ}$ C for 30 s followed by annealing and/or extension at 60  $^{\circ}$ C for 60 s (50 cycles), and finally inactivation at 98  $^{\circ}$ C for 10 min. Individual droplet end-point fluorescence signals in channel 1 (FAM) and channel 2 (HEX) were read using a QX100 Droplet Reader (Bio-Rad) and then analyzed with QuantaSoft analysis software (Bio-Rad).

## THEORY

**Predicting DNA Melting Thermodynamics Using a Nearest-Neighbor Type Model.** Measurements of the melting thermodynamics of either complementary DNA duplexes or LNA/DNA heteroduplexes are typically conducted in a standard thermodynamic solution comprised of pH 7 background buffer and 1 M NaCl.<sup>16,18,19,25</sup> Conversely, solutions employed in PCR detection of somatic mutations typically contain 20–100 mM NaCl or KCl. In addition, magnesium ( $Mg^{2+}$ ) is generally added to a concentration of 1–6 mM in PCR master mixes as a cofactor for Taq DNA polymerase. Both of these departures from the standard solution condition at which thermodynamic data are most often acquired affect duplex stability, as do other solution additives employed in amplification reactions. In particular, deoxyribonucleotide triphosphates (dNTPs) bind excess  $Mg^{2+}$ , while dimethyl sulfoxide (DMSO), which is added as a cosolvent to facilitate amplification of difficult templates, decreases  $T_m$ .<sup>26</sup> Finally, chemical modifications to oligonucleotides, including the addition of a reporter dye and a fluorescence quencher, affect  $T_m$ , as well.<sup>27</sup> A model capable of predicting probe properties under PCR-relevant conditions will therefore have to account for these various effects.

Recently, we reported a new model<sup>16</sup> that accurately predicts  $T_m$  values and melting thermodynamics for both complementary DNA homoduplexes and LNA/DNA heteroduplexes under standard conditions (pH 7, 1 M NaCl). Other models have also been described for this purpose.<sup>17–19</sup> They all compute the  $T_m$  of a short (<30 bp) complementary B-form duplex using the standard thermodynamic relation

$$T_m = \frac{\Delta H}{\Delta S - R \ln(C_T/4)} \quad (4)$$

where  $C_T$  is now divided by 4 because the two complementary strands are equimolar in concentration and the reaction must

therefore be treated as bimolecular. Differences between these various models arise primarily through the manner in which the thermodynamic changes,  $\Delta H$  and  $\Delta S$ , for the helix-to-coil transition are computed. It therefore is useful to segregate the available models into those that assume heat capacity change  $\Delta C_p$  for the melting transition is negligible (in part because accurate values for  $\Delta C_p$  have only recently been acquired) and those that account for the temperature dependence of  $\Delta H$  and  $\Delta S$  through a non-zero  $\Delta C_p$ . While either type of model can be extended to provide predictions of  $\Delta T_{m(MT-WT)}$  for probe design, the approach, parametrization, and output of the two approaches differ as described below. Before proceeding to that discussion, we note that a feature common to these models is that they are generally applicable to melting thermodynamics of the canonical B-form helical structure and may not provide accurate predictions for duplexes containing DNA sequences known to have a propensity for alternative conformations such as B\*-form and A-form helices associated with A-tract and G-tract sequence motifs, respectively.<sup>28</sup>

**Predicting  $T_m$  Values of LNA/DNA Heteroduplexes Using a  $\Delta C_p = 0$  Type Model.** Though other models have been described,<sup>17,18</sup> Owczarzy et al.<sup>19</sup> have arguably developed the most advanced zero- $\Delta C_p$  type model for predicting from sequence information the  $T_m$  of any short perfectly complementary duplex containing LNAs on one of the strands. Hereafter termed a type 1 model, it is based on the widely used unified nearest-neighbor thermodynamic (NNT) model of SantaLucia<sup>29</sup> and reduces to it when applied to pure-DNA duplexes. In type 1 models,<sup>19,29</sup> temperature-independent  $\Delta H$  and  $\Delta S$  values for complementary DNA/LNA heteroduplexes in standard thermodynamic solutions are computed as

$$\Delta H = \sum_{i=1}^2 n_i \Delta H_{EE_i} + \sum_{j=1}^{10} n_j \Delta H_{DNA_j} + \sum_{k=1}^{48} n_k \Delta \Delta H_{LNA_k} \quad (5)$$

$$\Delta S = \Delta S_{sym}^{\circ} + \sum_{i=1}^2 n_i \Delta S_{EE_i} + \sum_{j=1}^{10} n_j \Delta S_{DNA_j} + \sum_{k=1}^{48} n_k \Delta \Delta S_{LNA_k} \quad (6)$$

where  $\Delta S_{sym}^{\circ}$  is an exact result of statistical mechanics that applies only to self-complementary sequences and accounts for the fact that a bimolecular complex formed from two self-complementary strands has a 2-fold rotational symmetry that is not present in either of the single strands or any duplex formed from non-self-complementary strands.<sup>30,31</sup> In either equation, the first summation accounts for the unique energetics of terminal base pairs (end effects), with  $n_i$  specifying the number of terminal base pairs of type  $i$  in the duplex. The second summation accounts for the contribution to the melting energetics of the isosequential DNA duplex of each unique Watson–Crick nearest-neighbor base pair doublet of type  $j$ . There are 10 such unique doublets, and  $n_j$  counts the number of each in the duplex. The requirement for nearest-neighbor enthalpy ( $\Delta H_{DNA_j}$ ) and entropy ( $\Delta S_{DNA_j}$ ) parameters for each doublet is firmly supported by theory, most notably modified forms of the Poland–Sheraga Hamiltonian (see, for example, ref 32) that partition base pair formation and stacking interactions at the nearest-neighbor level to account for the unique nonlinear contributions of these two interactions to

duplex DNA stability. The third summation is more empirical in nature. It assumes that perturbations to duplex stability resulting from a DNA to LNA substitution also occur at the nearest-neighbor level, where  $n_k$  specifies the number of each of the 48 possible types of LNA-containing doublets that may be present in a duplex when LNA substitutions are restricted to only one of the two strands. The form of the summation therefore tacitly assumes that an LNA substitution perturbs not only base pair energetics but also base stacking interactions in a sequence-sensitive manner. While this assumption is certainly in keeping with the nearest-neighbor concept, it presents challenges in terms of both the physical meaning of the combined 96 new parameters (48  $\Delta H_{\text{LNA}_k}$  and 48  $\Delta S_{\text{LNA}_k}$  parameters) introduced into the model and the ability to regress a unique and reliable value for each of those parameters. Despite these concerns, type 1 models<sup>19</sup> are on average quite accurate in their  $T_m$  predictions for LNA/DNA heteroduplexes, as is the underlying unified NNT model of SantaLucia<sup>29</sup> when it is applied to pure-DNA homoduplexes.

**Predicting  $T_m$  Values of LNA/DNA Heteroduplexes Using a Model Based on a Non-Zero  $\Delta C_p$ .**  $T_m$  values for complementary DNA homoduplexes and LNA/DNA heteroduplexes may also be predicted using a model that accounts for the temperature dependence of  $\Delta H^\circ$  and  $\Delta S^\circ$ . The first such “type 2” model was described by Hughesman et al.<sup>16</sup> It accurately predicts melting thermodynamics of complementary duplexes containing any pattern of LNA substitutions on one of the strands. When applied to DNA homoduplexes under standard solution conditions, it differs from the unified NNT model by accounting for both a non-zero  $\Delta C_p$  and the unique base pairing energetics of terminal 5'-ta groups. Temperature-dependent  $\Delta H$  and  $\Delta S$  values for either pure-DNA homoduplexes or DNA/LNA heteroduplexes are computed as

$$\begin{aligned} \Delta H(T_m) &= \sum_{i=1}^2 n_i \Delta H_{\text{EE}_i}^\circ + \lambda \Delta H_{5'-\text{ta}}^\circ \\ &\quad + \sum_{j=1}^{10} n_j \Delta H_{\text{DNA}_j}^\circ + \Delta \Delta H_{\text{LNA}} \\ &\quad + \Delta C_p (T_m - T_{\text{ref}}) \\ &= \Delta H_{\text{DNA}}^\circ + \Delta \Delta H_{\text{LNA}} + \Delta C_p (T_m - T_{\text{ref}}) \end{aligned} \quad (7)$$

$$\begin{aligned} \Delta S(T_m) &= \Delta S_{\text{sym}}^\circ + \sum_{i=1}^2 n_i \Delta S_{\text{EE}_i}^\circ + \lambda \Delta S_{5'-\text{ta}}^\circ \\ &\quad + \sum_{j=1}^{10} n_j \Delta S_{\text{DNA}_j}^\circ + \Delta \Delta S_{\text{LNA}} + \Delta C_p \ln \left( \frac{T_m}{T_{\text{ref}}} \right) \\ &= \Delta S_{\text{DNA}}^\circ + \Delta \Delta S_{\text{LNA}} + \Delta C_p \ln (T_m / T_{\text{ref}}) \end{aligned} \quad (8)$$

where the parameters  $\Delta H_{5'-\text{ta}}^\circ$  and  $\Delta S_{5'-\text{ta}}^\circ$  correct the melting enthalpy and entropy, respectively, for each of the  $\lambda$  ( $\lambda = 0, 1$ , or 2) 5'-ta terminal nearest-neighbor doublets. When the model is applied to probe design, those terminal 5'-ta corrections are small and may be neglected. As a result, type 2 models primarily distinguish themselves from their type 1 counterpart through terms defining the temperature dependencies of  $\Delta H$  and  $\Delta S$ , as well as the manner in which energetic changes arising from LNA substitutions are treated. In eqs 7 and 8, all pure-DNA parameters, including the terminal base

pair parameters ( $\Delta H_{\text{EE}_i}^\circ$  and  $\Delta S_{\text{EE}_i}^\circ$ ) and the NNT parameters ( $\Delta H_{\text{DNA}_j}^\circ$  and  $\Delta S_{\text{DNA}_j}^\circ$ ), are specific to a reference temperature,  $T_{\text{ref}}$ , which is taken to be 53 °C for reasons explained previously.<sup>33</sup> The values of  $\Delta H$  and  $\Delta S$  at the  $T_m$  of the duplex are then computed from a defined reference state (deg) of the isosequential pure-DNA duplex at  $T_{\text{ref}}$  and under standard thermodynamic solution conditions using perturbation terms for LNA substitutions ( $\Delta \Delta H_{\text{LNA}}$  and  $\Delta \Delta S_{\text{LNA}}$ ), as well as two temperature-dependent terms, where  $\Delta C_p$  is given by  $n \Delta C_p^{\text{bp}}$ ; here,  $n$  is the number of base pairs in the duplex, and  $\Delta C_p^{\text{bp}}$  is 42 cal mol<sup>-1</sup> K<sup>-1</sup> bp<sup>-1</sup>.<sup>33</sup>

The perturbation term  $\Delta \Delta S_{\text{LNA}}$  is computed as

$$\Delta \Delta S_{\text{LNA}} = \sum_{i=1}^4 n_i \Delta \Delta S_{\text{LNA}_i} \quad (9)$$

where  $n_i$  is the number of LNA/DNA base pairs of type  $i$ . The four required  $\Delta \Delta S_{\text{LNA}_i}$  parameters have been previously reported<sup>16</sup> and account for the incremental change in entropy for a helix-to-coil transition resulting from substitution of a given DNA nucleotide with its corresponding LNA nucleotide. They were determined by model regression to calorimetry-derived data sets ( $\Delta G$ ,  $\Delta H$ ,  $\Delta S$ , and  $T_m$ ) for 43 LNA/DNA heteroduplexes and their corresponding isosequential DNA homoduplexes. Taking into account their standard errors, those data sets indicate that changes in  $\Delta S$  resulting from an LNA substitution are statistically significant at the individual base pair level, but not at the nearest-neighbor level. The data therefore indicate that, within experimental certainty, incremental changes in stacking interactions resulting from an LNA substitution do not depend on the type of nearest-neighbor base that stacks with the substituted LNA. For unlabeled oligonucleotides, LNA substitutions at terminal positions are generally ignored in calculating  $\Delta \Delta S_{\text{LNA}_i}$  in accordance with our data<sup>16</sup> and those of others<sup>34–36</sup> that show that an LNA substitution at a terminal position does not result in a significant change in duplex stability. However, in the case of labeled oligonucleotides such as hydrolysis probes, LNA substitutions made at the 5'- and/or 3'-end of the sequence are no longer considered terminal, as they are flanked by either a 5'-fluorescent dye or 3'-quencher; they are therefore included in calculating  $\Delta \Delta S_{\text{LNA}_i}$ .

$\Delta \Delta H_{\text{LNA}_i}$  is calculated from  $\Delta \Delta H_{\text{LNA}_i}$  parameters in an analogous manner. However, model regression to the 43-member UVM-derived data set yielded  $\Delta \Delta H_{\text{LNA}_i}$  parameters that are statistically insignificant, indicating that, within experimental certainty,  $\Delta \Delta H_{\text{LNA}_i}$  for all  $i$  may be assumed to carry zero value. Thus, if the temperature dependencies of  $\Delta H$  and  $\Delta S$  are taken into account through a non-zero  $\Delta C_p$ , we find that the change in duplex stability arising from an LNA substitution is entropically driven.<sup>16</sup>

## RESULTS AND DISCUSSION

**Comparing Basic Properties of the Two Types of Models.** Type 1 (zero  $\Delta C_p$ ) and type 2 (non-zero  $\Delta C_p$ ) models both provide accurate predictions of  $T_m$  for short complementary pure-DNA duplexes and LNA/DNA heteroduplexes. The difference is in how they achieve those results, in particular, the number of parameters they require (Table 1) and the values of  $\Delta H$  and  $\Delta S$  they compute to predict  $T_m$  using eq 4. To predict melting thermodynamics of complementary pure-

**Table 1. Comparison of Parameters Required in Type 1 and Type 2 Models When They Are Applied to  $T_m$  Calculations for Complementary Pure-DNA Homoduplexes, Pure-DNA Homoduplexes Containing a Mismatched Base Pair, Complementary LNA:DNA Heteroduplexes, or LNA:DNA Heteroduplexes Containing a Mismatched Base Pair**

duplex type	parameter	type 1 model	type 2 model
pure-DNA homoduplexes <sup>a</sup>	$\Delta C_p$		1
	$\Delta S_{sym}^o$	1	1
	$\Delta H_{EE_i}$ or $\Delta H_{EE_i}^o$	2	2
	$\Delta S_{EE_i}$ or $\Delta S_{EE_i}^o$	2	2
mismatched DNA duplex	$\Delta H_{DNA_i}$ or $\Delta H_{DNA_i}^o$	10	10
	$\Delta S_{DNA_i}$ or $\Delta S_{DNA_i}^o$	10	10
	$\Delta H_{DNA:MM_i}$	48	
	$\Delta S_{DNA:MM_i}$	48	
	$\Delta G_{DNA_i}^o$		10
	$\Delta G_{DNA:MM_i}^o$		48
total no. of parameters for DNA duplexes		121	84
LNA:DNA heteroduplexes	$\Delta \Delta H_{LNA_i}$	48	
	$\Delta \Delta S_{LNA_i}$ or $\Delta S_{LNA_i}^o$	48	4
mismatched LNA:DNA duplex	$\Delta \Delta H_{LNA:MM_i}$	96	
	$\Delta \Delta S_{LNA:MM_i}$	96	
	$\Delta \Delta G_{LNA:MM_i}^o$		12
	$\Delta \Delta G_{NN-LNA}^o / \Delta \Delta G_{NN-LNA}^o$		2
total no. of model parameters		409	102

<sup>a</sup>Parameters used to correct for 5'-ta sequences have not been included in this comparison as the correction is insignificant when these models are applied to dual-labeled hydrolysis probes.

DNA homoduplexes, the two model types require very similar parametrization as both are based on the unified NNT model of SantaLucia.<sup>29</sup> The type 2 model<sup>16</sup> utilizes one additional parameter,  $\Delta C_p$ , which is required to compute the temperature dependencies of  $\Delta H$  and  $\Delta S$ . One consequence of this is illustrated in Table 2, which compares thermodynamic properties of an internal cc/gg doublet (within a pure-DNA homoduplex) computed as a function of duplex melting temperature using each type of model. In type 1 models, the enthalpy of the doublet in its duplexed state relative to that in its denatured state,  $\Delta H_{cc/gg}$ , is taken to be temperature-independent. The melting entropy change for the doublet,  $\Delta S_{cc/gg}$ , is likewise invariate with temperature. This is, however, physically implausible, which was demonstrated by Searle and Williams,<sup>37</sup> who combined single-molecule stretching data with Zimm–Bragg theory<sup>38</sup> to find that the two-state transition describing melting of short duplex DNA can be described only

if the melting entropy of each doublet changes with temperature in accordance with a non-zero, positive-in-value  $\Delta C_p$ .

Indeed, there are now compelling data from multiple independent studies, most notably calorimetry studies, showing that  $\Delta C_p$  is non-zero and positive in value.<sup>16,33,39–46</sup> For short complementary duplexes melting above 45 °C, measured  $\Delta C_p^{bp}$  values lie between 30 and 60 cal K<sup>−1</sup> (mol of bp)<sup>−1</sup>.<sup>44</sup> The positive  $\Delta C_p$  is thought to arise in part because the denaturation of each antiparallel strand of a double helix proceeds via an overstretching transition that includes net changes in strand solvation.<sup>37</sup> Excellent correlations between changes in solvent-exposed surface area and the value have been described, most notably for proteins (for a review, see ref 47). Bases that remain stacked in the single strand following duplex denaturation are likely to produce relatively little net change in polar and nonpolar surface hydration, and thus little change in  $C_p$ , but those bases that do unstack undergo a concomitant change in their states of hydration, contributing to a positive  $\Delta C_p$ . Schwarz's lab<sup>48,49</sup> and Mrevlishvili et al.<sup>50</sup> have independently shown that single-stranded DNA exhibits broad changes in stacking structure with temperature, and that the duplex DNA denaturation reaction is accompanied by changes in hydration. Their findings align with a particularly elegant study by Spink and Chaires,<sup>51</sup> who combined UVM, circular dichroism, and vapor-pressure osmometry experiments to estimate that, on average, the melting of poly(A)-poly(T) duplex DNA results in the net exchange of four water molecules per base pair. Other contributions to  $\Delta C_p$  are thought to include changes in the conformations of bases and strands resulting from counterion condensation and other electrostatic effects.<sup>52</sup> Though questions remain regarding the precise magnitude of these various contributions,<sup>53</sup> current theory and data both indicate that unstacking events provide important, if not dominant, contributions to  $\Delta C_p$ , as summarized in the excellent review by Mikulecky and Feig.<sup>44</sup> Type 2 models exploit these findings through inclusion of a non-zero  $\Delta C_p$ ;  $\Delta H$  and  $\Delta S$  are therefore predicted to be dependent on temperature (Table 2), and we find that the inclusion of  $\Delta C_p$  terms is most valuable when one is specifically concerned with accurate prediction of  $\Delta H$  and  $\Delta S$ .

This is because  $\Delta G$  and  $T_m$  are less dependent on  $\Delta C_p$  than are  $\Delta H$  and  $\Delta S$ . As a result, NNT models that assume zero  $\Delta C_p$  accurately predict  $T_m$  values for pure-DNA duplexes, as was shown by SantaLucia in developing the unified NNT model.<sup>29</sup> Moreover, the two model types are equally accurate in their ability to predict  $T_m$  values for short LNA-containing heteroduplexes. However, by accounting for the temperature dependence of  $\Delta H$  and  $\Delta S$ , the type 2 model requires only four parameters (the set of  $\Delta \Delta S_{LNA_i}$  values) to fully describe perturbations to duplex energetics arising from LNA substitutions (see Table 1).<sup>16</sup> A total of 96 parameters are required

**Table 2. Comparison of Melting Thermodynamic Values under Standard Thermodynamic Conditions for the cc/gg Nearest-Neighbor Doublet Computed Using a Type 1 or Type 2 Model**

T (°C)	type 1 model ( $\Delta C_p = 0$ )			type 2 model ( $\Delta C_p \neq 0$ ) <sup>a</sup>		
	$\Delta G$ (kcal/mol)	$\Delta H$ (kcal/mol)	$\Delta S$ (cal mol <sup>−1</sup> K <sup>−1</sup> )	$\Delta G$ (kcal/mol)	$\Delta H$ (kcal/mol)	$\Delta S$ (cal mol <sup>−1</sup> K <sup>−1</sup> )
37	1.83	8.0	19.9	1.79	6.7	15.7
53	1.51			1.51	8.0	19.9
70	1.17			1.13	9.4	24.2

<sup>a</sup>Type 2 model calculations set  $\Delta C_p = 42$  cal (mol of bp)<sup>−1</sup> K<sup>−1</sup> and  $T_{ref} = 53$  °C.



for this purpose in type 1 models.<sup>18,19</sup> At the very least, this shows that equivalent predictive power can be captured in a much smaller set of model parameters when the temperature dependencies of  $\Delta H$  and  $\Delta S$  are addressed. More importantly, it argues that models of type 2, due to their significantly lower level of parametrization (see Table 1), are well suited for extension to permit quantitative prediction of  $\Delta T_{m,(\text{MT-WT})}$  values and the model-based design of dual-labeled hydrolysis probes for qPCR and dPCR genotyping assays.

**Type 2 Model Extension To Predict Changes in Pure-DNA Duplex Stability Due to Mismatched Base Pairs, Added End Groups, and Changes in Solution Conditions.** Equation 4 is derived from the fundamental relation for  $\Delta G$ , the Gibbs energy change for the helix-to-coil transition of a complementary pure-DNA duplex at a total strand concentration  $C_T$ . That Gibbs energy function can be extended to describe helix-to-coil transition energies for either DNA homoduplexes or LNA heteroduplexes bearing a mismatched base pair, a terminal fluorophore, and/or a fluorescence quenching agent, as well as for any such duplex solubilized in a nonstandard solution, through the introduction of perturbation ( $\Delta\Delta$ ) terms at the Gibbs energy level:

$$T_m = \left[ \Delta H_{\text{DNA}}^\circ + \Delta\Delta H_{f/q} + \Delta C_p(T_m - T_{\text{ref}}) + \Delta\Delta G_{\text{DNA:MM}} + \Delta\Delta G_{\text{LNA:MM}} \right] / \left[ \Delta S_{\text{DNA}}^\circ + \Delta\Delta S_{\text{LNA}} + \Delta\Delta S_{f/q} + \Delta\Delta S_{\text{salt}} + \Delta C_p \ln\left(\frac{T_m}{T_{\text{ref}}}\right) + R \ln\left(\frac{C_T}{4}\right) \right] \quad (10)$$

Computed as indicated in eqs 10 and 11,  $\Delta H_{\text{DNA}}^\circ$  and  $\Delta S_{\text{DNA}}^\circ$  apply to the fully complementary pure-DNA duplex under standard state conditions ( $T_{\text{ref}}$ , standard thermodynamic solution conditions). To this reference, a perturbation term ( $\Delta\Delta H_{f/q}$ ) is applied to correct  $\Delta H$  for the addition of a terminal fluorophore and fluorescence quenching agent. Perturbation terms are also applied to the melting entropy to correct for terminal fluorescence/quenching agents ( $\Delta\Delta S_{f/q}$ ), LNA substitutions ( $\Delta\Delta S_{\text{LNA}}$ ), and salts ( $\Delta\Delta S_{\text{salt}}$ ). Values for  $\Delta\Delta H_{f/q}$  and  $\Delta\Delta S_{f/q}$  were reported by Moreira et al.,<sup>27</sup> while  $\Delta\Delta S_{\text{LNA}}$  values needed to compute  $\Delta\Delta S_{\text{LNA}}$  using eq 9 were reported by Hughesman et al.<sup>16</sup> A modification to the method of von Ahsen et al.<sup>26</sup>

$$\Delta\Delta S_{\text{salt}} = 0.847 n_{\text{bp}} \log_{10}[\text{Na}_{\text{eq}}^+] \quad (11)$$

that is consistent with the temperature dependencies of  $\Delta H$  and  $\Delta S$  is used to compute  $\Delta\Delta S_{\text{salt}}$ , where  $n_{\text{bp}}$  is the number of base pairs in the duplex and  $[\text{Na}_{\text{eq}}^+]$  is the molar concentration of sodium ion equivalents, computed as

$$[\text{Na}_{\text{eq}}^+] = 0.1[\text{monovalent cations}] + 0.12 \sqrt{[\text{Mg}^{2+}] - [\text{dNTPs}]} \quad (12)$$

In eq 12,  $[\text{dNTPs}]$  is the total molar concentration of deoxyribonucleotide triphosphates in the sample.

The introduction of a mismatched DNA:DNA or DNA:LNA base pair into the duplex sequence is included as perturbation terms at the Gibbs energy level and computed as

$$\Delta\Delta G_{\text{DNA:MM}} = - \sum_{i=1}^{10} n_i \Delta G_{\text{DNA}_i}^\circ + \sum_{j=1}^{40} n_j \Delta G_{\text{DNA:MM}_j} \quad (13)$$

$$\Delta\Delta G_{\text{LNA:MM}} = \sum_{i=1}^{12} n_i \Delta\Delta G_{\text{LNA:MM}_i} + \Delta\Delta G_{5'\text{NN-LNA}} + \Delta\Delta G_{3'\text{NN-LNA}} \quad (14)$$

The first summation in eq 13 subtracts the Gibbs energy of each complementary nearest-neighbor DNA doublet  $i$  lost when the mismatch is formed. The second summation then adds to  $\Delta G$  the free energy contributions of the corresponding nearest neighbors containing the mismatch, where  $\Delta\Delta G_{\text{DNA:MM}_i}$  is the Gibbs energy of nearest-neighbor doublet  $j$  containing the mismatched DNA base pair.  $\Delta\Delta G_{\text{LNA:MM}_i}$  quantifies the incremental change in the transition energy if an LNA is substituted into the mismatched base pair to form an LNA:DNA mismatch of type  $i$ . A final set of incremental corrections in eq 14 is applied only in cases (defined more fully in a later section) where a mismatch is flanked by a neighboring LNA substitution on either its 5'-side ( $\Delta\Delta G_{5'\text{NN-LNA}}$ ) and/or 3'-side ( $\Delta\Delta G_{3'\text{NN-LNA}}$ ). The set of required  $\Delta G_{\text{DNA}_i}^\circ$  and  $\Delta G_{\text{DNA:MM}_i}$  parameters used in eq 13 is provided by SantaLucia et al.<sup>54</sup> Type 2 model  $\Delta\Delta G_{\text{LNA:MM}_i}$  parameters, all of which were determined in this work through regression of eq 13 to UVM data sets as described in Materials and Methods, are listed in Table 3. The values for  $\Delta\Delta G_{5'\text{NN-LNA}}$  and  $\Delta\Delta G_{3'\text{NN-LNA}}$  were likewise regressed and are  $-0.17$  and  $-0.55$  kcal mol<sup>-1</sup>, respectively, indicating that the introduction of LNAs directly adjacent to a mismatch favors the denatured state.

In the extended type 2 model embodied in eqs 10–14, perturbations to the stability of the reference duplex arising from the introduction of either a DNA base pair mismatch or

**Table 3. Regressed  $\Delta\Delta G_{\text{LNA:MM}_i}^\circ$  Parameters and Associated Experimental  $\Delta\Delta T_m$  Values (eq 3) for All Possible Mismatched LNA:DNA Base Pairs (LNA and DNA bases shown in uppercase and lowercase letters, respectively)**

mismatch	$\Delta\Delta T_m$ (°C)	$\Delta\Delta G_{\text{LNA:MM}_i}^\circ$ (kcal/mol)
purine-purine		
A-a	$2.7 \pm 1.6$	$-0.50 \pm 0.27$
A-g	$3.4 \pm 3.1$	$-0.63 \pm 0.33$
G-a	$6.7 \pm 1.5$	$-1.18 \pm 0.25$
G-g	$4.4 \pm 1.6$	$-0.82 \pm 0.27$
pyrimidine-pyrimidine		
C-c	$2.9 \pm 1.7$	$-0.59 \pm 0.38$
C-t	$2.1 \pm 1.5$	$-0.44 \pm 0.24$
T-c	$1.7 \pm 0.9$	$-0.35 \pm 0.15$
T-t	$1.4 \pm 1.1$	$-0.32 \pm 0.20$
purine-pyrimidine		
A-c	$0.4 \pm 2.2$	$-0.11 \pm 0.28$
G-t	$-2.5 \pm 1.6$	$0.38 \pm 0.28$
pyrimidine-purine		
C-a	$0.4 \pm 1.2$	$-0.17 \pm 0.41$
T-g	$1.6 \pm 1.1$	$-0.28 \pm 0.20$

an LNA:DNA base pair mismatch are defined at the Gibbs energy level. In contrast, in corresponding type 1 models for mismatched pure-DNA homoduplexes<sup>25,55–58</sup> and for mismatched LNA-substituted heteroduplexes,<sup>19</sup> new values for  $\Delta H$  and  $\Delta S$  are computed for the mismatched duplex by replacing the enthalpic and entropic contributions of the lost complementary doublets with those of the corresponding doublets bearing the mismatch. As shown in Table 1, when applied to a pure-DNA homoduplex bearing a mismatched base pair, this approach requires an additional 48 enthalpic parameters and 48 entropic parameters to account for the contributions to  $\Delta H$  and  $\Delta S$  of all possible doublets containing a single mismatched base pair. While consistent with the NNT concept, many (~40%) of these added  $\Delta H_{\text{DNA:MM}_i}$  and  $\Delta S_{\text{DNA:MM}_i}$  parameters are not statistically significant, creating the possibility for anomalies in  $T_m$  predictions for mismatched duplexes.<sup>25,55–58</sup> This is reflected in Table 4, which reports as a

**Table 4. Duplex-to-Denatured State Thermodynamic Changes under Standard Thermodynamic Conditions for Complementary and Mismatched Nearest-Neighbor Pure-DNA Doublets Computed as a Function of Temperature using a Type 1 Model<sup>a</sup>**

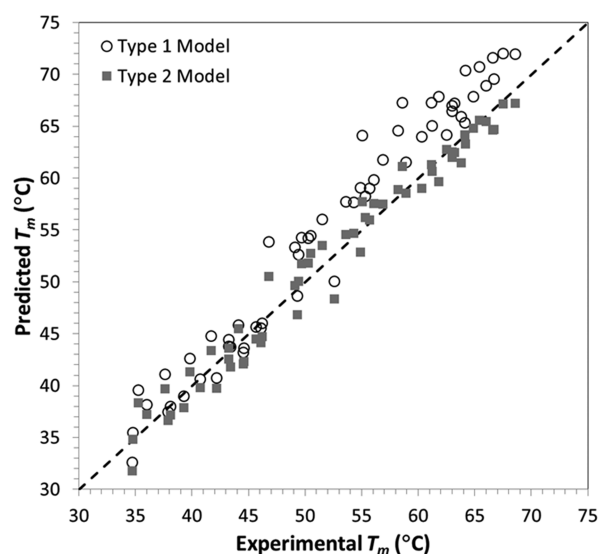
doublet	$\Delta H$	$\Delta S$	$\Delta G_{37^\circ\text{C}}$	$\Delta\Delta G_{70-37^\circ\text{C}}$
Complementary				
cg/cg	10.6	27.2	2.16	−0.90
cc/gg	8.0	19.9	1.83	−0.66
Mismatched				
tg/ct	5.0	15.8	0.10	−0.52
ac/tt	−0.7	−0.2	−0.64	0.01
tc/gg	−3.3	−10.4	−0.07	0.34
cc/ga	−5.2	−14.2	−0.80	0.47
aa/tc	−7.6	−20.2	−1.33	0.67

<sup>a</sup>Nearest-neighbor parameters used for the calculation taken from ref 54 and references therein.

function of temperature the melting thermodynamics of both complementary and mismatched pure-DNA doublets computed using a type 1 model. For the two perfectly matched doublets, that model predicts that at 37 °C the duplex state of the doublet is thermodynamically favored over the denatured state (i.e.,  $\Delta G_{37^\circ\text{C}} > 0$ , where  $\Delta$  indicates the duplex-to-denatured state transition). The model also predicts, in accordance with all experimental data for duplex DNA melting, that the denatured state of the doublet becomes increasingly favored as the temperature is increased; that is, the model predicts  $\Delta\Delta G_{70-37^\circ\text{C}} < 0$ . However, for several mismatched doublets, the type 1 model predicts a different trend that is at odds with available experiment. If the mismatched tc/gg doublet is taken as an example, the model captures the destabilizing effect the mismatch has on the duplexed doublet at 37 °C (i.e.,  $\Delta G_{37^\circ\text{C}} < 0$ ). However, it erroneously predicts that the duplexed state of the doublet becomes more stable with an increase in temperature ( $\Delta\Delta G_{70-37^\circ\text{C}} > 0$ ), such that it is thermodynamically favored at 70 °C (i.e.,  $\Delta G_{70^\circ\text{C}} = 0.27$  kcal mol<sup>−1</sup>).

In contrast, all  $\Delta G_{\text{DNA}_i}^\circ$  and most (89%)  $\Delta\Delta G_{\text{DNA:MM}_i}$  parameters are statistically significant, with those  $\Delta\Delta G_{\text{DNA:MM}_i}$  parameters that are not generally lying just inside their reported standard deviation.<sup>25,55–58</sup> As a result, we find that mismatch corrections are more quantitatively reliable when they are

applied at the Gibbs energy level. This is reflected in Figure 1 and Table S2 (Supporting Information), which compare the



**Figure 1.** Comparison of  $T_m$  values predicted by a type 1<sup>25,55–58</sup> or type 2 model to corresponding experimental  $T_m$  data for 60 pure-DNA homoduplexes containing one or two mismatched base pairs.

performance of our extended type 2 model (eqs 10–14) to that of a corresponding type 1 model<sup>25,55–58</sup> when they are applied to a large set of pure-DNA duplexes containing one or two isolated mismatched base pairs. While the performance of the two models is similar for mismatched duplexes melting at a  $T_m$  of  $\leq 50$  °C, the type 1 model overpredicts  $T_m$  for more stable duplexes containing one or two mismatched base pairs due, at least in part, to the unusual temperature dependence that model ascribes to the stabilities of certain mismatched doublets (see Table 4).

Finally, in the application of eqs 10–14 to the prediction of  $T_m$  values for duplexes containing a mismatch, it is important to note that the calculation may be performed by specifying either of two different duplexes as the reference state. Figure S1 (Supporting Information) shows that our type 2 model predictions are independent of that choice.

**Predicting Stabilities of Duplexes with One or More Mismatched LNA:DNA Base Pairs.** Melting thermodynamic data (Table S1, Supporting Information) under standard conditions for a set of 384 duplexes containing either a central LNA:DNA base pair mismatch or the corresponding DNA base pair mismatch were collected and used to regress  $\Delta\Delta G_{\text{LNA:MM}_i}$  parameters for all possible mismatched LNA:DNA base pairs (Table 3). The data were also used to compute mean  $\Delta\Delta T_m$ ,  $[\Delta T_{m(\text{LNA-LNA:MM}_i)} - \Delta T_{m(\text{DNA-DNA:MM}_i)}]$  values, as defined in eq 3, for all possible mismatched LNA:DNA base pairs. As noted previously,<sup>6</sup> LNAs are generally more energetically intolerant to mismatch formation, and this is reflected in the generally positive values of  $\Delta\Delta T_m$ , which indicate that nearly all LNA:DNA base pair mismatches are indeed more destabilizing to a duplex when compared to their corresponding DNA mismatch; the one exception, as noted by You et al.,<sup>6</sup> is the G-t mismatch. Our data show that this hyperdestabilization effect favoring the denatured state is largest for purine:purine LNA:DNA mismatches (Table 3).



You et al.<sup>6</sup> have reported data showing that the effect of a mismatched pure-DNA base pair (or LNA:DNA base pair) on duplex stability can be altered by a neighboring LNA substitution directly before (B; i.e., on the 5'-side) or after (A; 3'-side) the mismatch. Table 5 presents those data in a

**Table 5. Average Net Effect on Duplex Melting Temperatures of LNA Substitutions Directly before (B), Directly after (A), and/or within (M) a DNA:DNA (m) Base Pair Mismatch<sup>a</sup>**

type of LNA substitution	$\Delta T_m$ (°C) <sup>b</sup>		
	experiment <sup>c</sup>	base model <sup>d</sup>	corrected model <sup>e</sup>
DNA mismatch (m)			
B-m	0.6 ± 1.3	-0.1 ± 0.0	0.4 ± 0.0
m-A	1.2 ± 1.1	-0.1 ± 0.0	1.5 ± 0.0
B-m-A	1.8 ± 1.5	-0.2 ± 0.0	1.9 ± 0.0
LNA mismatch (M)			
M	1.6 ± 1.6	1.2 ± 1.1	1.2 ± 1.1
B-M <sup>f</sup>	1.4 ± 2.0	1.1 ± 1.1	1.1 ± 1.1
M-A	2.8 ± 1.8	1.1 ± 1.1	2.7 ± 1.1
B-M-A <sup>d</sup>	3.0 ± 1.9	1.0 ± 1.1	2.6 ± 1.1

<sup>a</sup>Performance of eq 10 in capturing this effect when  $\Delta\Delta G_{5'NN-LNA}^\circ$  and  $\Delta\Delta G_{3'NN-LNA}^\circ$  parameters are included in eq 14 or not. Data used for analysis taken from ref 6. <sup>b</sup>All  $\Delta T_m$  values reported are under standard thermodynamic conditions and are relative to the  $T_m$  of the corresponding mismatched pure-DNA duplex containing no B, M, or A type LNA substitutions. <sup>c</sup>For each type of LNA substitution, the mean  $\Delta T_m$  and the range of  $\Delta T_m$  values observed experimentally are reported. <sup>d</sup>Mean error and standard deviation of model predictions using eqs 10–14 with  $\Delta\Delta G_{5'NN-LNA}^\circ$  and  $\Delta\Delta G_{3'NN-LNA}^\circ$  parameters set equal to zero. <sup>e</sup>Mean error and standard deviation of model predictions using eqs 10–14 with  $\Delta\Delta G_{5'NN-LNA}^\circ$  and  $\Delta\Delta G_{3'NN-LNA}^\circ$  parameters set equal to -0.17 and -0.54 kcal mol<sup>-1</sup>, respectively. <sup>f</sup>The  $\Delta\Delta G_{5'NN-LNA}^\circ$  parameter is not applied to B-M type sequences.

manner that shows that the destabilization of a duplex containing a pure-DNA mismatch is enhanced by an LNA substitution either directly before or after the mismatch, with the latter substitution having the larger destabilizing effect. Moreover, the data show that this hyperdestabilizing effect is additive in cases in which the mismatch is flanked on both sides by an LNA substitution. Most LNA substitutions within a mismatch are also seen to hyperdestabilize the duplex. Further destabilization is then observed for a neighboring LNA substitution on the 3'-side of the mismatch, but not on the

5'-side. Finally, Table 5 shows that these various destabilizing effects can be captured quantitatively in the type 2 model through the inclusion of two additional parameters,  $\Delta\Delta G_{5'NN-LNA}^\circ$  and  $\Delta\Delta G_{3'NN-LNA}^\circ$ , and the provision that  $\Delta\Delta G_{5'NN-LNA}^\circ$  not be applied to cases in which the mismatch and the 5'-neighboring base pair both contain an LNA substitution.

Table 6 reports the performance of our extended type 2 model when it is applied to four different classes of duplexes: fully complementary pure-DNA duplexes, fully complementary duplexes containing one or more LNA substitutions, unsubstituted duplexes containing one or two mismatched base pair(s), and LNA-substituted duplexes containing one or two DNA:DNA and/or LNA:DNA mismatched base pair(s). None of the sequences included in this table were used to regress model parameters. All possible LNA:DNA and mismatched LNA:DNA base pairs are presented at least three times in the data sets. For each class of duplex, the results presented therefore represent a true test of model accuracy. In each column, the average experimental  $T_m$  and the range of experimental  $T_m$  values for the duplexes are reported along with the mean error and standard deviation of model predictions for the entire set of sequences within that class. In each case, model accuracy is very good, showing a low standard deviation and a mean error of <1 °C. As a result, the model is able to accurately predict  $\Delta T_{m(PM-MM)}$  for both pure-DNA duplexes and DNA:LNA heteroduplexes. In addition, the model accurately predicts  $\Delta\Delta T_m$  (eq 3), thereby allowing one to reliably assess the impact that LNA substitutions at or near the site of variance will have on the specificity of a probe. Data and model results used to generate Table 6 are provided in Table S3 (Supporting Information).

**Application of the Model to Predicting and Improving the  $\Delta T_{m(PM-MM)}$  of Allele-Specific Hydrolysis Probes through LNA Substitutions.** As our type 2 NNT model is accurate in predicting melting thermodynamics under standard conditions for both pure-DNA duplexes and LNA-substituted duplexes (Table 6), we asked if the model might also be used to accurately predict  $T_m$  and  $\Delta T_{m(PM-MM)}$  values for LNA-substituted dual-labeled hydrolysis probes. Model corrections for PCR solution conditions and for the presence of both a fluorophore (reporter) and a fluorescence quenching agent are therefore required. In our model, eqs 11 and 12 are used to correct for changes in solution composition [salt concentrations, added magnesium ion (Mg<sup>2+</sup>)] away from standard

**Table 6. Performance of Our Model (eqs 10–14) in Predicting  $T_m$  (degrees Celsius) under Standard Thermodynamic Conditions of Pure-DNA Duplexes and DNA/LNA Heteroduplexes Formed with Templates That Are Fully Complementary or Harbor One or Two Isolated (non-neighboring) Base Pair Mismatches**

	DNA:PM	DNA:MM	LNA:PM	LNA:MM
no. of unique duplexed sequences	12	31	23	55
experimental $T_m$ <sup>a</sup>	68.5 ± 6.9	54.1 ± 10.0	76.7 ± 9.9	63.0 ± 10.6
error in model predictions <sup>b</sup>	0.2 ± 1.0	-0.4 ± 1.4	-0.7 ± 1.2	-1.3 ± 2.4
experimental $\Delta T_{m(DNA:PM-DNA:MM)}$ or $\Delta T_{m(LNA:PM-LNA:MM)}$		12.2 ± 3.8		14.4 ± 4.3
error in model predictions <sup>b</sup>		0.0 ± 1.6		0.4 ± 2.2
experimental $\Delta\Delta T_m$ (eq 6)			2.2 ± 2.4	
error in model predictions <sup>b</sup>			0.0 ± 1.8	

<sup>a</sup>Experimental  $T_m$  values for each class of duplex are reported as the mean  $T_m$  values for all sequences ± the average range of  $T_m$  values recorded for the set of duplexes. All  $T_m$  data were collected under standard thermodynamic solution conditions (1 M NaCl in pH 7 buffer) and a  $C_T$  of 2 or 50 μM (Table S3 of the Supporting Information and data from refs 6 and 19). <sup>b</sup>Total errors in model predictions for a given class of duplex are reported as mean errors ± the standard deviation.

**Table 7. Comparison of Experimental (UVM) and Model-Predicted Melting (duplex dissociation) Thermodynamics for Unlabeled and Dual-Labeled LNA-Substituted Probes under PCR-Relevant Solution Conditions**

probe		experimentally measured by UVM <sup>b</sup>						model-predicted					
target	sequence (5' to 3') <sup>a</sup>	LNA (%)	c/g (%)	$\Delta G^{37}$ (kcal/mol)	$\Delta H^{\circ}$ (kcal/mol)	$\Delta S^{\circ}$ (eu) <sup>d</sup>	$T_m$ (°C)	$T_m^{PCR}$ (°C) <sup>c</sup>	$\Delta G^{37}$ (kcal/mol)	$\Delta H^{\circ}$ (kcal/mol)	$\Delta S^{\circ}$ (eu) <sup>d</sup>	$T_m$ (°C)	$T_m^{PCR}$ (°C) <sup>c</sup>
unlabeled probes													
EGFR WT exon 20	aTcACGcagCTca	38	54	18.0 ± 0.0	106.5 ± 0.6	282.5 ± 1.8	68.9 ± 0.2	65.4	18.7	108.5	286.5	71.0	67.5
EGFR T790M	aTcATGcagCTca	46	46	17.9 ± 0.1	103.9 ± 0.6	274.5 ± 1.8	69.3 ± 0.0	65.7	18.3	105.1	276.7	70.7	67.1
EGFR WT exon 21	agcAggttgccAgcc	13	63	20.8 ± 0.3	131.1 ± 2.2	351.6 ± 6.2	71.4 ± 0.1	68.5	20.5	134.8	365.2	68.9	66.1
EGFR WT exon 21	ggcTggccaaacTgct	13	63	21.2 ± 0.2	132.4 ± 2.1	354.4 ± 6.2	72.2 ± 0.1	69.3	21.1	135.9	366.6	70.6	67.8
EGFR L858R	tgcccCgCcca	18	82	17.9 ± 0.3	93.8 ± 3.2	241.6 ± 9.3	73.8 ± 0.1	69.7	17.2	91.0	235.5	71.3	67.1
EGFR L861Q	aCCcagcTgTTt	42	50	16.3 ± 0.1	93.2 ± 0.4	245.8 ± 0.9	66.3 ± 0.3	62.4	17.3	95.0	248.0	70.1	66.2
PIK3CA WT exon 10	ctGaaatCactGagCa	31	44	19.1 ± 0.1	119.5 ± 1.2	320.3 ± 3.3	69.2 ± 0.1	66.0	20.2	131.5	355.6	68.9	66.0
PIK3CA WT exon 21	atgCaCATCatggt	36	43	18.5 ± 0.2	105.1 ± 2.1	275.7 ± 6.2	72.0 ± 0.1	68.4	18.8	112.3	298.4	70.0	66.6
PTEN WT exon 5	gggACGAAcTgg	50	67	17.9 ± 0.3	94.5 ± 2.6	243.9 ± 7.4	73.5 ± 0.1	69.4	18.0	100.7	264.1	70.7	67.0
TP53 WT exon 7	cacACGCaCct	45	64	17.3 ± 0.4	89.8 ± 4.5	231 ± 13.1	72.6 ± 0.3	68.3	17.4	92.9	241.0	71.2	67.1
dual-labeled probes													
BRAF V600E	FAM-agatttCTcGTaG-C-BHQ1	33	40	19.5 ± 0.3	121.3 ± 1.7	324.6 ± 4.3	71.2 ± 0.1	67.0	20.3	122.4	325.6	72.2	69.1
JAK2 V617F	FAM-ctccACagAAaCatac-BHQ1 <sup>e</sup>	31	44	20.7 ± 0.4	136.1 ± 4.0	367.9 ± 11.8	72.6 ± 0.2	67.0	19.7	132.4	359.7	70.4	64.7
JAK2 V617F	FAM-acaGAAACATACT-BHQ1	77	31	19.7 ± 1.1	110.6 ± 10.0	288.8 ± 28.9	78.7 ± 0.6	71.6	19.2	106.0	275.1	79.3	71.9
KIT WT exon 17	HEX-ccagaGACATCaag-BHQ1	43	50	18.9 ± 0.6	112.8 ± 6.1	299.1 ± 17.6	73.2 ± 0.2	67.4	18.4	112.3	299.5	70.9	65.6
KIT D816V	FAM-ccagaGTCATC-BHQ1	55	55	17.4 ± 0.3	98.2 ± 0.7	258.0 ± 1.4	72.3 ± 0.4	65.4	16.3	88.8	231.2	70.8	64.1
KIT D816V	FAM-ccagaGTCaTCaag-BHQ1	36	50	19.8 ± 0.1	121.7 ± 1.0	324.7 ± 3.0	73.3 ± 0.0	67.9	19.0	115.8	308.8	71.7	66.6

<sup>a</sup>FAM = 6-carboxyfluorescein; HEX = hexachlorofluorescein; BHQ1 = Black Hole Quencher 1. LNA substitutions are capitalized. <sup>b</sup>Experimental data were measured by the UVM method in PCR buffer containing 50 mM K<sup>+</sup> and 3 mM Mg<sup>2+</sup>; the data were collected at a C<sub>T</sub> of 2 μM for all probes except for experiments involving KIT and JAK2 probes that were performed at C<sub>T</sub> values of 5 and 10 μM, respectively. <sup>c</sup>Experimental  $T_{m,PCR}$  determined using eq 15 with a C<sub>T</sub> of 0.2 μM. <sup>d</sup>eu = entropy unit (calories per mole per kelvin). <sup>e</sup>Previously reported probe designed by Markova et al.<sup>9</sup>

thermodynamic conditions. More comprehensive models are available for this purpose,<sup>59</sup> but we have found that eq 11, which we derived from the work of von Ahsen et al.,<sup>26</sup> provides a reliable estimate for the effect of solution composition on  $T_m$ . Similarly, the values of  $\Delta\Delta H_{f/q}$  and  $\Delta\Delta S_{f/q}$  used in eq 10 to correct  $T_m$  for reporter and fluorescence quenching groups were reported by Moreira et al.<sup>27</sup>

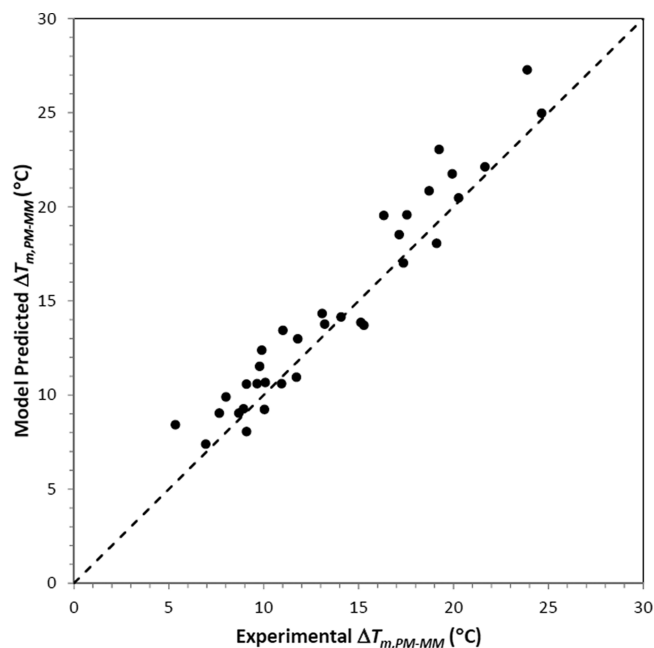
Table 7 reports LNA-substituted unlabeled and dual-labeled hydrolysis probes designed using our type 2 model to target known somatic point mutation “hot spots” in clinically relevant genes associated with various cancers, including *EGFR*, *PIK3CA*, *PTEN*, *TP53*, *BRAF*, *JAK2*, and *KIT*. These targets cover a broad range of sequence diversity (c/g content ranging from 31 to 82%), and the probes designed against them contain different LNA contents (ranging from 13 to 77%) as well as different LNA substitution patterns. Each probe was designed to contain LNA(s) at the site of variation(s) to take advantage of the greater thermodynamic penalty for an LNA:DNA mismatch (Table 5), as well as multiple LNA substitutions at other positions that collectively serve to decrease probe length while maintaining the  $T_m$  of the duplex formed by the probe and its perfect complement at a value between 65 and 70 °C under PCR conditions. In PCR, the initial probe concentration, and thus  $C_T$  (because the probe is in great excess), is typically set at (or near) 0.2  $\mu\text{M}$  ( $C_{T,\text{PCR}}$ ), a value that is too low to permit direct measurement of melting thermodynamics by the UVM method. However, the melting temperature for each probe:template duplex can be measured by UVM under PCR conditions and a somewhat higher  $C_T$  ( $C_{T,\text{Expt}}$ ), and then corrected to  $C_{T,\text{PCR}}$  using the rigorous two-state bimolecular melting thermodynamics relation

$$T_{m,\text{PCR}} = \frac{\Delta H_{\text{Expt}} + \Delta C_p(T_{m,\text{PCR}} - T_{m,\text{Expt}})}{\Delta S_{\text{Expt}} + \Delta C_p \ln(T_{m,\text{PCR}}/T_{m,\text{Expt}}) - R \ln(C_{T,\text{PCR}}/2)} \quad (15)$$

where  $\Delta H_{\text{Expt}}$ ,  $\Delta S_{\text{Expt}}$ , and  $T_{m,\text{Expt}}$  are the UVM-measured values at  $C_{T,\text{Expt}}$ .  $C_{T,\text{PCR}}$  is divided by 2 in eq 15 because the probe is in great excess during PCR. For the set of 16 LNA-bearing probes, model-predicted  $T_m$  values at  $C_{T,\text{PCR}}$  agree well with experiment, having a low total mean error and a standard deviation of  $-0.6 \pm 2.0$ . Moreover, at  $C_{T,\text{Expt}}$ , the model not only accurately predicts  $T_m$  ( $-0.7 \pm 2.0$ ) but also provides accurate estimates of  $\Delta G^\circ_{37}$ ,  $\Delta H^\circ$ , and  $\Delta S^\circ$  with average errors (predicted – experimental) determined to be  $0 \pm 4$ ,  $1 \pm 5$ , and  $1 \pm 6\%$  (mean error  $\pm$  standard deviation), respectively.

To confirm the ability of the model to predict the discrimination [ $\Delta T_{m(\text{PM-MM})}$ ] of single LNA/DNA base pair mismatches in LNA-bearing probes, UVM data were also collected on a total of 34 different mismatched probe:template duplexes. All 12 unique single LNA/DNA base pair mismatches were represented one or more times in this data set, and a good agreement between experimentally determined and model-predicted  $\Delta T_{m(\text{PM-MM})}$  values was found (Figure 2), with a mean error of  $0.9 \pm 1.4$  °C. Together, the results presented in Table 7 and Figure 2 demonstrate the general utility of the model in predicting melting thermodynamics of probes under PCR-relevant conditions and, more importantly, in designing LNA substitution patterns in allele-specific probes to achieve an effective  $\Delta T_{m(\text{MT-WT})}$  by increasing the destabilizing effect of a mismatch through an LNA-mediated decrease in probe length.

**Quantitative Droplet Digital PCR Detection of the *BRAF* V600E or *KIT* D816V Mutation Using a Single**



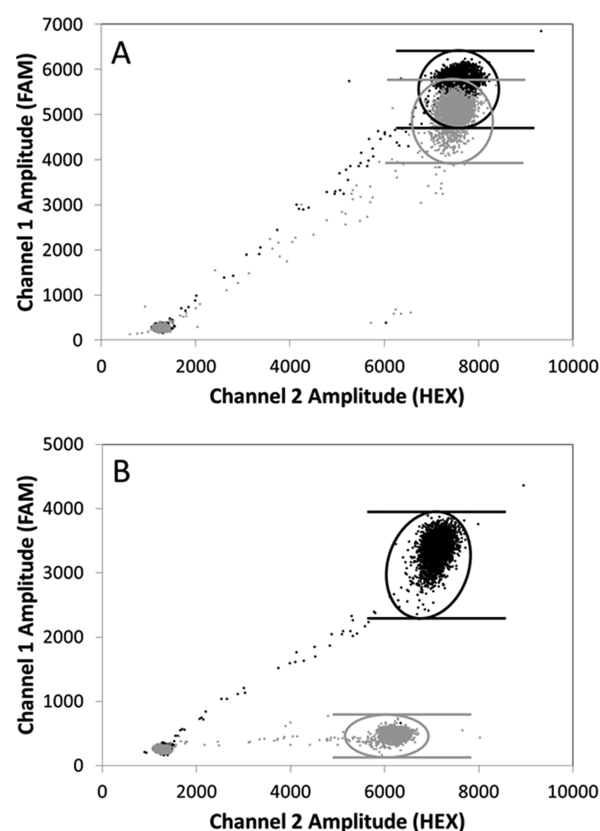
**Figure 2.** Comparison of experimental and model-predicted  $\Delta T_{m,\text{PM-MM}}$  values for 34 mismatched probe:template duplexes.

**Mutant-Specific Hydrolysis Probe.** The ability of the model-designed LNA-substituted allele-specific (AS) probes to enhance the selective detection of a mutant allele was demonstrated in a ddPCR assay using the LNA-substituted probe directed against *BRAF* V600E. Quantitative ddPCR detection of the MT *BRAF* V600E (c. 1799T > A) allele in a background of WT *BRAF* requires complete segregation of output data fields (clusters) for the two alleles. Figure 3A shows that significant overlap of *BRAF* V600E and WT *BRAF* data clusters occurs when the ddPCR assay utilizes a conventional pure-DNA AS probe against *BRAF* V600E (5'-FAM-catcgagatttctctgtagctagacc-IBFQ-3') designed using our model. When targeting a MT allele harboring a single somatic point mutation, pure-DNA AS probes often offer a  $\Delta T_{m(\text{MT-WT})}$  of approximately  $\leq 6$  °C. Indeed, the pure-DNA probe against *BRAF* V600E provides experimental and predicted  $\Delta T_{m(\text{MT-WT})}$  values of 4.3 and 5.0 °C, respectively, which are too small for achieving complete segregation of data fields when  $T_a$  is set at a typical value of 60 °C.

When the LNA-substituted P15L6 probe against *BRAF* V600E, which offers experimental and predicted  $\Delta T_{m(\text{MT-WT})}$  values of 11.7 and 10.9 °C, respectively (Table S4, Supporting Information), is employed instead, complete segregation of MT and WT data fields is achieved at a  $T_a$  of 60 °C (Figure 3B), permitting quantitative detection of MT allele frequency within the sample.

Given that the pure-DNA AS probe against *BRAF* V600E does offer some thermodynamic discrimination, improved segregation of MT and WT data fields can be achieved by increasing  $T_a$  to a value closer to the  $T_{m,\text{PM}}$  for that probe under PCR conditions. For example, at a  $T_a$  of 64 °C, reasonable segregation of MT and WT data clusters is achieved (Figure 4A). Nevertheless, it is unlikely that a cancer testing laboratory would adopt an assay in this form because of its strong sensitivity to small perturbations in  $T_a$ . In contrast, the performance of the LNA-substituted probe is relatively





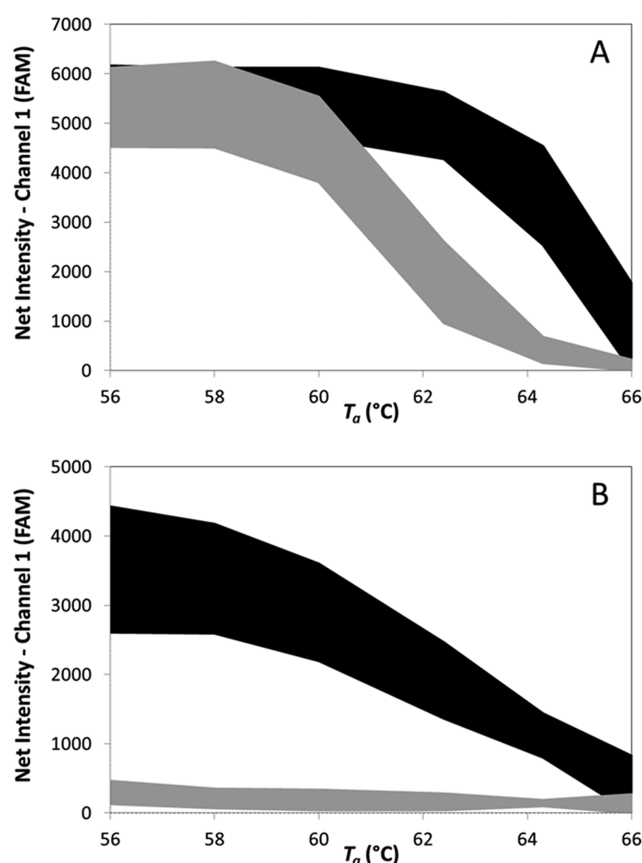
**Figure 3.** Detection and discrimination by ddPCR performed at a  $T_a$  of 60 °C of plasmids harboring either the WT *BRAF* (gray) or MT *BRAF* V600E (black) gene utilizing either (A) a *BRAF* V600E pure-DNA AS DNA probe (5'-FAM-catcagagatttctctgtagtagacc-IBFQ-3') or (B) the *BRAF* V600E (5'-FAM-agatttCTCtGTagC-BHQ1-3') LNA-substituted AS probe (Table 7). Horizontal lines indicate the upper and lower limits of each data cluster (circled). The cluster in the bottom right corner of each graph represents empty droplets.

insensitive to  $T_a$ , providing for complete segregation of data fields over a wide range of  $T_a$  values (Figure 4B).

Finally, we note that the model may be applied to the effective design of either pure-DNA or LNA-substituted AS probes. This is illustrated in Figure 5, which reports overlap of MT and WT data fields as a function of  $T_a$  for a ddPCR assay against *KIT* D816V utilizing either a model-designed pure-DNA AS probe (5'-FAM-ttggtctagccagagtcacagaa-IBFQ-3') with experimental and predicted  $\Delta T_{m(MT-WT)}$  values of 6.0 and 6.6 °C, respectively, or a model-designed LNA-substituted AS probe (5'-FAM-ccagaGTCaTCaag-BHQ1-3') with experimental and predicted  $\Delta T_{m(MT-WT)}$  values of 15.3 and 13.7 °C, respectively (Table S4, Supporting Information). While the LNA-substituted probe provides complete segregation of MT and WT data fields over a wide range of  $T_a$  values, the performance of the model-designed pure-DNA probe is sufficiently robust to yield an assay that potentially could satisfy clinical standards.

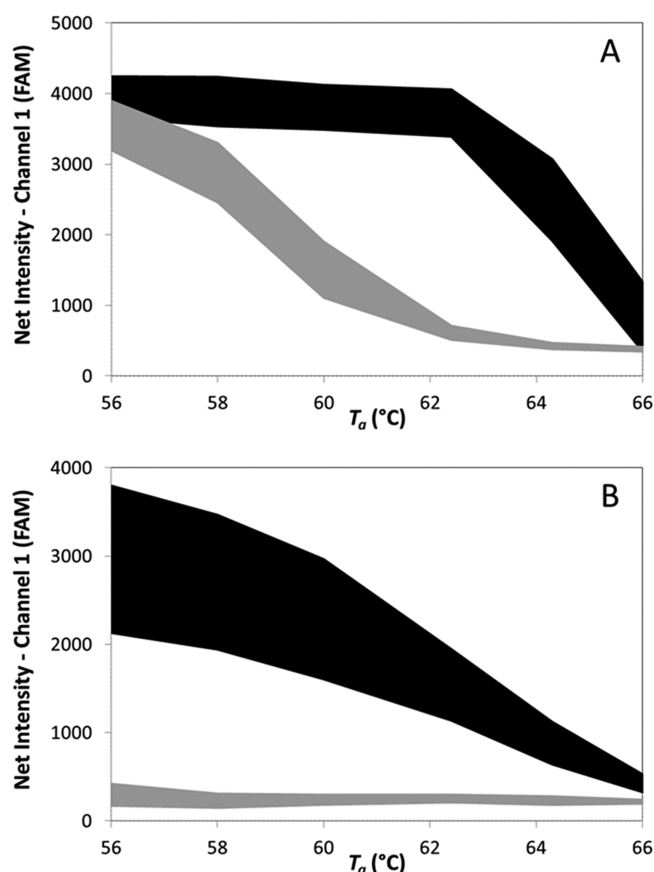
## CONCLUSIONS

Real-time monitoring using dual-labeled hydrolysis probes has allowed the development of a wide range of PCR-based laboratory procedures and also improved the extent and reliability of information that can be obtained from patient specimens. Clinical applications of real-time PCR have grown exponentially, and the emergence of dPCR and useful modified



**Figure 4.** Ribbon diagram defining the discrimination of WT *BRAF* (gray) and MT *BRAF* V600E (black) data fields as a function of  $T_a$  in a ddPCR assay utilizing either (A) a *BRAF* V600E pure-DNA AS DNA probe (see Figure 2) or (B) the *BRAF* V600E LNA-substituted AS probe (Table 7). The upper and lower limits of each normalized data field (see Figure 2) define the span of each band shown. For either allele, normalized channel 1 (FAM) intensity values were determined by subtracting the upper and lower bounds of the empty droplet cluster from the corresponding upper and lower bounds of the data cluster.

probe chemistries, including LNA substitutions, is offering the potential to further expand diagnostic applications of PCR through their ability to improve quantification and differentiation of amplification products. However, fully realizing this potential will require model-based methods for designing probes and predicting their hybridization thermodynamics as a function of their sequence, chemistry, and template complementarity. Here, we have shown that formal accounting of the temperature dependence of  $\Delta H$  and  $\Delta S$  for the melting transition can be used to develop a nearest-neighbor thermodynamic model that accurately predicts the melting thermodynamics of a short oligonucleotide duplexed either to its perfect complement or to a template containing a mismatched base pair. The model may be applied to pure-DNA duplexes or to duplexes for which one strand contains any number and pattern of LNA substitutions. Perturbations to duplex stability arising from mismatched DNA:DNA or LNA:DNA base pairs are treated at the Gibbs energy level to maintain statistical significance in the regressed model parameters. As hydrolysis probe sequences are typically comprised of mixtures of all NNs, the model developed here is specifically designed to treat duplexes that are B-form in helix structure in their complementary unsubstituted (no LNA)



**Figure 5.** Ribbon diagram defining the discrimination of WT *KIT* (gray) and MT *KIT* D816V (black) data fields as a function of  $T_m$  in a ddPCR assay utilizing either (A) a *KIT* D816V pure-DNA AS DNA probe (5'-FAM-ttggtctagccagatcatcaagaa-IBFQ-3') or (B) the *KIT* D816V LNA-substituted AS probe (5'-FAM-ccagaGTCaTCaag-BHQ1-3') (Table 7). The upper and lower limits of each normalized data field (see Figure 2) define the span of each band shown. For either allele, normalized channel 1 (FAM) intensity values were determined by subtracting the upper and lower bounds of the empty droplet cluster from the corresponding upper and lower bounds of the data cluster.

isosequential state. The model is therefore not specifically designed to treat duplexes containing substantial A-tract (i.e., consecutive aa/tt or at/at NNs) or G-tract (consecutive c/g base pairs) sequence motifs. Nevertheless, it predicts  $T_m$  and melting thermodynamics of short A-tract rich duplexes reasonably well, deviating from experimental  $T_m$  values, for example, by no more than  $\pm 3^\circ\text{C}$  for short duplexes containing up to six consecutive AA/TT NNs. This result is not surprising, as the B\*-form helix associated with A-tract sequence motifs is structurally similar to the classic B-form helix. Poorer agreement is observed when the model is applied to short complementary duplexes high in G-tract content; deviations from experimental  $T_m$  values as large as  $\pm 6.6^\circ\text{C}$  are observed. This is consistent with the fact that G-tract sequences tend toward a modified A-form structural motif in which the sizes of the major and minor grooves of the duplex are reversed relative to those within the B-form helix. NNT parameters specific to B-form helix energetics and entropy are therefore not expected to be applicable to this significantly altered helix structure.

When appropriate equations are introduced to correct for changes in solution conditions and terminal addition of fluorescent dyes and quenchers, the model may be used to

predict and thereby tailor the  $T_m$  of a pure-DNA or LNA-substituted hydrolysis probe when duplexed either to its perfect-match template or to a template harboring a non-complementary base. The model therefore should be of use to clinicians and biologists needing to design probes that unequivocally distinguish and quantify two closely related alleles in either a qPCR or a dPCR assay. This potential was demonstrated by showing that the model could be used to design AS probes that completely discriminate and quantify either *BRAF* V600E and WT *BRAF* templates or *KIT* D816V and WT *KIT* templates in a ddPCR assay.

## ■ ASSOCIATED CONTENT

### Supporting Information

Additional supplemental tables and figures. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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### Notes

The authors declare no competing financial interest.

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